Practical Exercise:
Asymmetric Key Cryptography (RSA)

October 16, 2019

Due date: no date

Changelog

• v1.0 - Initial Version.

Introduction

In order to elaborate this laboratory guide it is required to install the Java Development Environment (JDK) or Python 3.

The examples provided will use both Java and Python. For Python you need to install the cryptography module.

1 Key generation

Implement a small program to generate a pair of asymmetric keys to be used with the RSA algorithm. The program should accept the key size (1024, 2048, 3072, or 4096) as the first argument, and create the key with this size. Once having the keys, the program should write the public key to a file specified as the second argument, and the private key to a file specified as the third argument.

Therefore the program should be executed as:

```
java AsymKeys 1024 public.key private.key
```

The basic structure of such program in Java will be:

```
KeyPairGenerator kpg = KeyPairGenerator.getInstance( "RSA" );
kpg.initialize( keySize );
KeyPair keyPair = kpg.generateKeyPair();
```

Tip: use the classes

- java.security.KeyPairGenerator
- java.security.KeyPair

and the interfaces

- java.security.PrivateKey
- java.security.PublicKey

For Python consider the execution of the program with different parameters, namely a password for protecting the key file and a single file name with the PEM extension:

python3 asym_keys.py 1024 password key.PEM

The basic structure of such program in Python will be:

2 Ciphering with the RSA algorithm

Implement a second program to cipher the content of a file using the RSA algorithm and the PKCS #1 OAEP (Optimal Asymmetric Encryption Padding) padding. The program should accept three arguments: the first is the name of the file containing the (public) key to use; the second is the name of the file containing the clear text file to cipher; and the third is the name of the file to write the ciphertext.

Tip: you can use less arguments and consider the use of STDIN and STDOUT in the absence of file specifications.

The basic structure of such program in Java will be:

```
Cipher cipher = Cipher.getInstance ( "RSA/ECB/OAEPWithSHA-1AndMGF1Padding" );
cipher.init( Cipher.ENCRYPT_MODE, publicKey );

// clearText must be a byte array
cryptogram = cipher.doFinal(cleartext);
```

Tip: use the classes

- java.security.KeyFactory,
- javax.crypto.Cipher
- \bullet java.security.spec. X509EncodedKeySpec.

Note: Take in consideration that a specific key size will impose a specific block size, which limits the amount of bytes that cleartext can have. Take a look at the getBlockSize method of the javax.crypto.Cipher class. Only use small files with the appropriate size. The methods to handle larger files will be addressed in section 4.

Tip: for saving both private and public key contents in a single PEM file you can consider using the Bouncy Castle package¹.

The basic structure of such program in Python will be:

¹https://www.bouncycastle.org

```
from cryptography.hazmat.primitives import hashes
from cryptography.hazmat.primitives import serialization
from cryptography.hazmat.primitives.asymmetric import padding
from cryptography.hazmat.backends import default_backend
# Load key pair to a PEM file protected by a password
with open( key_filename, "rb" ) as kf:
    priv_key = serialization.load_pem_private_key( kf.read(),
                                                     bytes ( password, "utf-8" ),
                                                     default_backend() )
pub_key = priv_key.public_key()
# Calculate the maximum amount of data we can encrypt with OAEP + SHA256
maxLen = (pub_key.key_size // 8) - 2 * hashes.SHA256.digest_size - 2
# Read for plaintext no more than maxLen bytes from the input file
# Encrypt the plaintext using OAEP + MGF1(SHA256) + SHA256
ciphertext = pub_key.encrypt( plaintext,
                                padding.OAEP( padding.MGF1( hashes.SHA256() ),
                                                 hashes.SHA256(), None ) )
# Write ciphertext in the ouput file
```

3 Deciphering with the RSA algorithm

Implement a second program to decipher the content of a file using the RSA algorithm. The program should accept three arguments: the first is the name of the file containing the (private) key to use; the second is the name of the file containing the ciphertext file to decipher; and the third is the name of the file to write the clear text.

Tip: use the classes

- java.security.KeyFactory
- javax.crypto.Cipher
- java.security.spec.PKCS8EncodedKeySpec

as well as the interface

• java.security.**PrivateKey**.

Note: for the Python program you may have to use an extra argument, a password, to get access to the private key stored inside the key file.

4 How to cipher a big file?

As referred previously, when using RSA the maximum number of bytes that can be successfully ciphered is limited by the key size. For a key with 1024 bits and OAEP with SHA-1, that maximum is 86 bytes². For other paddings the maximum is different; for instance, for PKCS #1 v1.5 it is 117 bytes³. This is a major limitation of RSA as the size of most files, emails, and Web pages are well above this value.

A simple solution would be to break the input text in blocks, each with 86 bytes, and cipher the blocks independently. This is the approach followed when using the ECB approach in symmetric ciphers (but now without the pattern repetition problem exemplified in the last class – explain why!!).

 $^{^{2}86 = 128 - 2 \}times 20 - 2$, where 20 is the SHA-1 output length.

 $^{^{3}117 = 128 - 11}$

Moreover, RSA is very slow in comparison with the symmetric algorithms. As an example, in a commonly available laptop, it is possible to do 7254 sign (cipher) operations per second with RSA-1024, while it is possible to do 8 million cipher operations over 128 bits when using AES-128-CBC⁴.

Therefore, the use of RSA for ciphering big texts (more than one block) is discouraged. Can you propose a solution for quickly securing a large file with RSA, so that only the owner of a given public key can decipher it? Maybe by combining different algorithms (AES and RSA)?

Implement the respective hybrid cipher and decipher programs and evaluate your solution.

5 Implementing the RSA algorithm

While the implementation of cryptographic algorithms for use in final applications is discouraged, in relation to use well known, publicly available and properly reviewed libraries, implementing the RSA algorithm is a simple task with educational value.

The RSA key generation process can be quickly described according to the following steps. Take in consideration that in Java, manipulation of large integers can be done with the java.math.BigInteger.

- Generate two (large) random primes, P and Q, of approximately equal size. The BigInteger class provides a method (probablePrime) which generates probable primes with a given bit length. Take in consideration the P and Q are just part of the key. Therefore these prime numbers must be about half the size of the desired key;
- Compute $N = P \times Q$. You can use the standard multiplication of the BigInteger class;
- Compute $Z = (P-1) \times (Q-1)$. You can use the standard multiplication of the BigInteger class;
- Choose an integer E, 1 < E < Z, such that GCD(E, Z) = 1. GDC is the Greatest Common Divisor and is supported by the BigInteger class;
- Compute the secret exponent D, 1 < D < Z, such that $E \times D \equiv 1 \mod Z$. This can be computed using the modInverse method (e.g, D = E.modInverse(Z))
- The public key is the tuple $\langle N, E \rangle$ and the private key is the tuple $\langle N, D \rangle$.

After the keys are generated, the algorithm supports two operations: cipher and decipher. Remember that the clear text is handled as a BigInteger, even if the clear text is some text file.

Ciphering a text requires computing $c = t^E \mod N$

Deciphering a cipherText requires computing $t = c^D \mod N$

Where c is the ciphertext, t is the clear text, D, E, N represent the key components.

Implement a program generating a key pair and then using the keys to cipher and decipher a clear text. Consider the method modPow of the BigInteger class for ciphering and deciphering.

Note: In this example we are skipping the implementation of any padding before encryption, and unpadding (and validation) upon decryption, which usually takes place when using RSA.

References

- 1. RSA Cryptography Specifications Version 2.0, http://tools.ietf.org/html/rfc2437
- $2. \ \ Basic \ \ RSA \ \ example, \ \ \textbf{http://www.java2s.com/Tutorial/Java/0490_Security/BasicRSAexample.} \\ \ \ \ \textbf{htm}$

⁴You can check your laptop running openss1 speed